How can a physical universe produce mathematical minds?
And why are they so hard to replicate in current AI systems?

SPEAKER
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EXTENDED ABSTRACT:
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This is a progress report on a long-term project. Most theories of learning assume there’s a fixed type of world to be understood by learners, whereas biological evolution, in collaboration with its products, is metaphysically creative, constantly extending the diversity and complexity of the world to be understood, using ever expanding forms of compositionality, requiring increasingly complex mathematical mechanisms in understanders. (Its powers and achievements exceed all other known examples of creativity, including the forms of "transformational creativity" in humans discussed by Margaret Boden.) Extending the types of learners adds to the mathematical complexity of what needs to be understood, especially in recently evolved learners trying to understand themselves. Human mathematical competences are not yet understood well enough, to be modelled or replicated (despite fashionable claims), though Immanuel Kant identified some key aspects of the
Background: Evolution -- the blind mathematician

It is not widely appreciated that as evolution produces increasingly complex organisms, with increasingly complex behaviours, it uses increasingly sophisticated mathematical discoveries. There are infinitely many different mathematical structures of different kinds, including: Boolean logic, the natural numbers (0, 1, 2, 3, 4, ...), the positive ratios (1/2, 1/3, 2/3, 1/4, ...), groups and other algebraic structures, Euclidean geometry, the topological (non-metrical) subset of Euclidean geometry, negative feedback and other information-based control structures, the probability space for "throws" of N perfectly balanced six sided dice, and Turing's "universal" computing machine.

These structures are abstract structured types, that exist whether or not physical instances of those types exist, and whether or not any thinkers notice or make use of their existence.

Among the mathematical structures/types "discovered" and used by biological evolution are designs for increasingly complex organisms, for types of mechanism used by such organism, and types of information used for control, e.g. control of reproduction, control of growth, control of temperature, control of chemical balances, and, more obviously, control of motivation, perception, learning, communication, and many more.

E.g. use of negative-feedback control loops to keep systems within safe parts of their state-space, or to move them toward desirable states or away from undesirable states, is commonplace in organisms, though human engineers (e.g. James Watt, who invented the Watt centrifugal speed governor for steam engines) did not discover and use such control structures until millions of years after they began to be used by evolution and its products.

Not all such information-based control mechanisms need to use precise numerical values. E.g. sometimes it is enough to be able to detect whether something is changing, or whether it is increasing or decreasing, or whether the rate of increase or decrease is changing, or whether one object is moving toward or away from another, or whether some object is moving into or out of a particular volume of space. (Evolution can be more broad-minded than some science teachers.)

[ I use "information" in the sense of novelist Jane Austen, not Claude Shannon, as explained here: http://www.cs.bham.ac.uk/research/projects/cogaff/misc/austen-info.html ]

In more complex organisms, evolution discovered the power of layered epigenetic mechanisms that use different mathematical structures (including new combinations of simpler structures) at different stages of development. As a result, recently evolved sophisticated learners have multi-stage, "meta-configured" genomes [2], whose later stages of gene expression produce more complex, more recently evolved, more mathematically complex and abstract, discovery and learning mechanisms with different evolutionary histories. The best known example of this is the collection of different developmental transitions in (signed, spoken and written) language "learning" capabilities. (Strictly, these are language creation capabilities, which is why there are so many different human languages.)

If humans had to learn languages, instead of being able to create them (cooperatively), then the thousands of known human languages could not have existed, because there were originally no language users to learn from, at least not on this planet.
A meta-configured genome repeatedly produces new learning powers within each developing individual. The "layered" developmental processes are depicted crudely in this diagram (joint work with Jackie Chappell):

Multiple routes from genome to behaviours

A key feature is that the specific powers produced during development are not all specified in the genome: some of them, e.g. later acquisition of skills and knowledge, are absorbed from aspects of the environment influenced by ancestors, e.g. results of prior stages of cultural evolution, or changes in other species, as illustrated by evolved symbiosis.

E.g. in 2019, development in many young children is strongly influenced by computer based products of older generations who did not have access to those products when they were children.
Likewise, when I was a child (in the 1940s-1950s) my development was strongly influenced by others who had written books on Euclidean geometry, whereas a few thousand years earlier there were no teachers with knowledge of Euclidean geometry nor books on Euclidean geometry. The minds of humans in those days had significant gaps that were filled in later generations by the works of mathematicians who made new discoveries and produced teaching practices and materials passing on those discoveries.
(Some of those discoveries are no longer taught in all schools because of misguided educational decisions in the 20th Century. As a result there are now many AI researchers and knowledge engineers whose minds lack important relevant information that had been removed from their school syllabus.)

Some of the more recently evolved parts of the human genome produce enormously varied adult competences, including inventive powers that cannot result simply from a uniform learning mechanism presented with examples of invention[3].
Despite impressive recent results, nothing in current AI matches or explains the evolved types of spatial intelligence found in squirrels, weaver birds, elephants, human toddlers and ancient mathematicians, e.g. Archimedes, Euclid, Zeno, and others. (That’s why I’ll refuse to use a self-drive car in cluttered busy urban environments.) Current psychology and neuroscience also lack the required explanatory power.

These claims will be supported by a collection of examples, including spatial reasoning competences of pre-verbal toddlers, squirrels, nest-building birds, and others.

Partly inspired by Immanuel Kant and Alan Turing I’ll outline a research programme, the Meta-Morphogenesis project, aiming to fill deep gaps in our scientific and philosophical theories, including perhaps chemistry-based extensions to Turing-computability[4], which Turing himself implied might be needed in his PhD Thesis.

   A collection of examples: http://www.cs.bham.ac.uk/research/projects/cogaff/misc/impossible.html

using ideas developed in collaboration with Jackie Chappell.

[3] Compare uses of spatial intelligence in our ancestors to make deep mathematical discoveries (e.g. in geometry and topology) and recent advances in theoretical physics that those ancient thinkers could not have produced.


**Video of related talk**


**Boden: Three types of creativity**

Margaret Boden has famously distinguished (at least) three types of creativity:
(i) making unfamiliar, but in some way valuable, combinations of familiar ideas
(ii) exploring new regions of a conceptual space
(iii) transformational creativity (including creating new conceptual spaces)
For an introduction see this abstract: https://www.researchgate.net/publication/209436199_Creativity_in_a_nutshell

**Additional references (all work in progress)**

The Turing-Inspired Meta-Morphogenesis Project
http://www.cs.bham.ac.uk/research/projects/cogaff/misc/meta-morphogenesis.html
http://www.cs.bham.ac.uk/research/projects/cogaff/misc/construction-kits.html
http://www.cs.bham.ac.uk/research/projects/cogaff/misc/super-turing-geom.html
Compositionality in evolution’s products:
http://www.cs.bham.ac.uk/research/projects/cogaff/misc/compositionality.html
http://www.cs.bham.ac.uk/research/projects/cogaff/misc/m-m-overview.html
An account of how Science and Philosophy (Metaphysics) share a deep concern for investigation of what sorts of things are possible and how they are possible, can be found in Chapter 2 of my 1978 Book (The Computer Revolution in Philosophy), now online, partially updated: 
http://www.cs.bham.ac.uk/research/projects/cogaff/crp/#chap2

Some of these ideas are related to, and have been influenced by, the Birmingham FraMEPhys project, @FraMEPhys.

The Meta-configured genome idea was developed in collaboration with Dr Jackie Chappell https://www.birmingham.ac.uk/staff/profiles/biosciences/chappell-jackie.aspx