

A Very Simple Big-Step λ -Interpreter

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Code - Type Definitions

```
type debruijn =  
  Lambda of debruijn |  
  Index of int |  
  App of debruijn * debruijn |  
  Const of int;;  
  
type value =  
  Closure of debruijn * value list |  
  Con of int;;
```

Code - The Lookup Function

```
let rec index n xs =  
  match xs with  
  x::ys ->  
    if n = 1 then x  
    else index (n - 1) ys;;
```

Code - The Eval Function (Interpreter)

```
let rec eval exp env =  
  match exp with  
  | Const n ->  
    Con n |  
  | Index n ->  
    index n env |  
  | Lambda body ->  
    Closure (body, env) |  
  | App (funct, argument) ->  
    match eval funct env with  
    | Closure (body, env2) ->  
      let argval = eval argument env in  
      eval body (env2 @ [argval]);;
```

Code - Tests

```
let t1 = Lambda (Lambda (Index 2));;  
let t2 = App (t1, t1);;  
let t3 = App(App(t1, Const 666), Const 777);;  
let t4 = App(t2, t3);;  
eval t4 [];
```

```
let t5 = Lambda (Lambda (App (Index 1, Index 2)));;  
let t6 = Lambda (Index 1);;  
let t7 = App (t5, t6);;  
let t8 = App (t7, Const 5);;  
eval t8 [];
```

```
let o1 = Lambda (App(Index 1, Index 1));;  
let omega = App(o1, o1);;  
eval omega [];
```