

The Genetic Programming Collaboration Network and its Communities

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ABSTRACT

Useful information about scientific collaboration structures and patterns can be inferred from computer databases of published papers. The genetic programming bibliography is the most complete reference of papers on GP. In addition to locating publications, it contains coauthor and coeditor relationships from which a more complete picture of the field emerges. We treat these relationships as undirected small world graphs whose study reveals the community structure of the GP collaborative social network. Automatic analysis discovers new communities and highlights new facets of them. The investigation reveals many similarities between GP and coauthorship networks in other scientific fields but also some subtle differences such as a smaller central network component and a high clustering.

Categories and Subject Descriptors

I.2 [Artificial Intelligence]: Automatic Programming; I.7 [Document and Text Processing]: General

General Terms

Human Factors

Keywords

Genetic Programming, Collaboration Networks, Coauthorship Networks, Communities

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1. INTRODUCTION

The genetic programming (GP) bibliography¹, created and maintained by one of us (WBL) and by S. Gustafson contains most of the GP papers. As such, it is a rich source of data that implicitly describes many aspects of the structure of the GP community. Searching the bibliography and looking at the images² provides a lot of useful information about the field and the people working on GP. However, a deeper analysis of the data, that goes beyond the mere pictorial aspect, provides a much more complete view. The coauthorship data is a social network since collaborating in a research study usually requires that the coauthors become personally acquainted. Thus, studying those ties, their structure, and their evolution allows a better understanding of the factors that shape scientific collaboration.

We present a systematic study of the GP coauthorship data base using methods and tools pertaining to complex networks and social network analysis. Social network analysis (see [12] for a survey), although it is an old discipline, has recently received new impetus and tools from the field of complex networks (see [10] for an excellent review). This is mainly due to the relatively recent availability of large machine-readable databases such as the GP bibliography. Social acquaintances involve psychological and other human aspects that are difficult to quantify. However, as it has been done in other fields [3, 5, 7, 8], we use objective data such as joint published work to stand for social bonds. Since this must ignore subtler aspects of a collaboration relationship, it is obviously far from perfect as a social indicator, yet it is still a good “proxy” for the network of social relationships and can reveal several interesting facts and trends.

A preliminary investigation of the GP coauthorship network appears in [13]. In the first part of this article we update this initial study using the most recent data and adding the study of the influence of excluding co-edited proceedings and books. In the second part we offer a new analysis of the finer community structure of the collaboration network. Similar studies have been performed in the last few years on several other collaboration networks in disciplines such

¹<http://www.cs.bham.ac.uk/~wbl/biblio/>

²<http://www.cs.bham.ac.uk/~wbl/biblio/gp-coauthors/>

as physics, mathematics, medicine, biology, and computer science [3, 5, 7, 8]. A related investigation concerning the EC collaboration network [4] has appeared recently in popular form, but it does not take into account, for example the community structure of the network. [4] deals with some of the same statistical features for the EC community at large as we describe in detail here for GP. The values reported by [4] are in line with those found here for the GP field. Given that the intersection between the GP researchers and general EC is likely to be rather large, it would be interesting to study how they are related to each other.

2. THE GP COLLABORATION NETWORK

We treat the genetic programming social network as a graph where each node is a GP researcher, i.e. someone who has at least one entry in the bibliography. There is a connection between two people if they have coauthored at least one paper, or if they have coedited one or more book or proceedings. As of the start of 2007, there is a total of $N = 2809$ connected nodes, i.e. authors that have at least one GP collaborator, and a total of 5853 edges (collaborations) in the GP coauthorship network. There are 367 isolated vertices, which represent authors who have not collaborated with others to the extent of coauthoring a paper. Isolated vertices are ignored in our graph statistics. We have also excluded a single paper with 108 coauthors in a nuclear physics journal. This is because we consider it to be an anomalous entry that is not representative of typical collaborations in our discipline.

Due to the youth of GP, the graph is relatively small compared to some studied collaboration networks [3, 5, 7]. (Although some published studies have covered much smaller and more specialised networks, e.g. of only 50 people [2].) The main disadvantage of studying a relatively small database is that, like any statistical study, more data allows deeper and more meaningful inferences to be drawn. In particular, studies of the form of the distributions (such as whether they follow exponential or power laws) require a large amount of data. The advantages include that the graph almost fully represents the state of the whole GP community. This allows reliable characterisation of collaboration in the community. Also, the problems of multiple authors with the same name (e.g. A. Smith), outliers and different name spelling that plague the larger data sets, are unlikely and easy to spot in our data.

Although in many cases in our field co-editing a book or proceedings volume does reflect personal acquaintance, there are some large coeditorships which are not representative and so may give a slanted view. Therefore in the following figures we present two kinds of statistics: those that include all joint publications and those in which co-edited conference proceedings and co-edited books are excluded (but not their contents, of course). Next we present and discuss some basic measures that characterise the GP collaboration network.

2.1 Number of Papers per Author

The average number of papers per author is 3.16 with co-edited books and proceedings and it is 3.14 without. The five most prolific authors are, in decreasing order: J. Koza, R. Poli, W. B. Langdon, W. Banzhaf and C. Ryan. If we exclude proceedings' co-editors the ranking remains unchanged. Naturally the distribution of the number of pa-

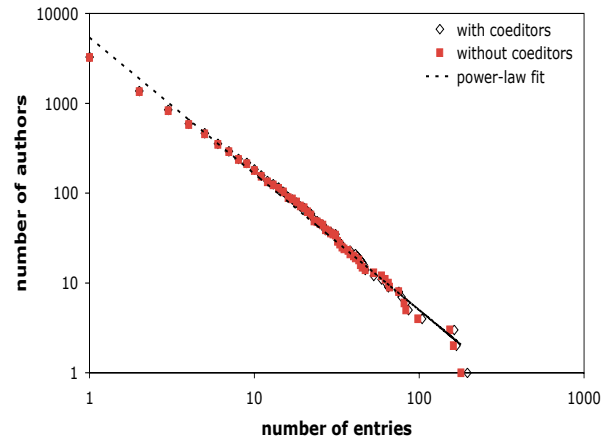


Figure 1: Cumulative distribution of the number of entries per author. Log-log scale. The straight line is the best mean-square fit and shows the number of authors is $\propto k^{-2.5}$.

pers per author, $P(k)$, has some scatter, particularly in the tail of the distribution. Thus, we present in Figure 1 the graph of the cumulative distribution $P(k \geq n)$ which is smoother and allows the same inferences to be made. The curves are rather well fitted by a straight line, and thus the distributions follow a power-law $P(k) \propto k^{-\gamma}$ with a calculated exponent γ of 2.5 for both of them. A power-law distribution with similar exponents has been observed for analogous collaboration networks, e.g. 2.86 for a biological publication database (Medline), 3.41 for a computer science database (NCSTRL), 2.4 for mathematics, and 2.1 for a neuroscience papers database [3, 7]. A smaller exponent (in absolute value) means that the tail of the distribution is more stretched towards high values of degree.

2.2 Number of Collaborators per Author

The average number of collaborators per author, i.e. the mean degree $\langle k \rangle$ of the coauthorship graph, is 4.17 with proceedings and 3.62 without. This is close to the values reported by studies of computer science, physics (excluding high energy physics) and Mathematics, suggesting GP follows similar collaboration patterns to those disciplines. However it is much less than found in high energy physics and medicine. See Table 1. In order and including co-edited volumes, the five authors that have the largest number of collaborators are: W. Banzhaf, J.A. Foster, P. Nordin, W.B. Langdon, U.-M. O'Reilly. Without co-edited books the ranking is: P. Nordin, W. Banzhaf, J. Daida, C. Ryan and R. Goodacre. The five "pairs" that have the highest number of coauthored papers are, in decreasing order both with or without co-edited proceedings: J. Koza-M. A. Keane, R. Poli-W.B. Langdon, J. Koza-D. Andre, J. Koza-F. Bennet and F. Bennet-M.A. Keane. This shows that J. Koza's group has been tightly collaborating for a long time, a conclusion that is confirmed in the community study of section 4. It is also evident that the W.B. Langdon-R. Poli association has been an extremely productive one.

Figure 2 shows the cumulative distributions of the number of collaborators. One sees that the distributions are not pure power-laws, otherwise the points would approximately lie on

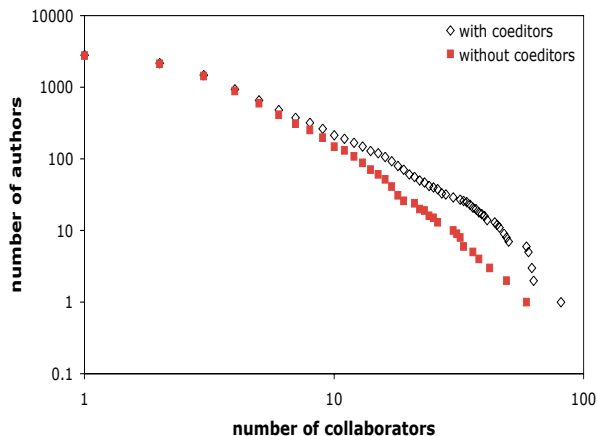


Figure 2: Cumulative distribution of the number of authors with a given number of collaborators. Logarithmic scale on both axes.

a straight line. Rather, the distributions shows a power-law regime in the first part followed by an exponential decay in the tail. That is, the whole network cannot be fitted by a power-law. This is quite common. In fact, several measured social networks do not follow a power-law degree distribution [1, 7] and are best fitted either by an exponential degree distribution $P(k) \approx e^{-k/\langle k \rangle}$ or by an exponentially truncated power-law of the type $P(k) \approx k^{-\gamma} e^{-k/k_c}$, where k_c represents a critical connectivity and $\langle k \rangle$ is the average degree.

2.3 Number of Authors per Paper

Figure 3 shows the cumulative distribution of the number of papers written by a given number of coauthors. Here the distribution also has a tail that is longer than that of a Gaussian or exponential distribution, however it does not follow a power-law. The average number of authors per paper is 2.25 (2.22 without co-editors). From Table 1 we can see that these figures are close to the equivalent ones for computer science (NCSTRL) and physics, while Mathematics has a lower number of co-authors per paper. On the other hand, nuclear physics stands out with an unusually high number of coauthors per paper.

From Figures 2 and 3 one can see that the tails of the distribution with co-editors are longer than without them. Thus, taking co-editorship into account seems to rather artificially inflate the number of publications with many co-authors and, by consequence, the number of collaborators that a person has.

2.4 Connected Components

In the theory of Poisson random graphs there is a critical value of average degree $\langle k \rangle = 1$ above which there is a sudden appearance of a *giant component*. This is so-called since most vertices belong to it. The other components are smaller and have an exponentially decreasing size distribution [10]. Although collaboration graphs are not random, a similar phenomenon appears. Including coeditors there are 1025 GP authors in the giant component. This is 36.5% of the total graph. If we exclude coediting proceedings etc. the size is 743, representing the 26.9% of the total. In the giant

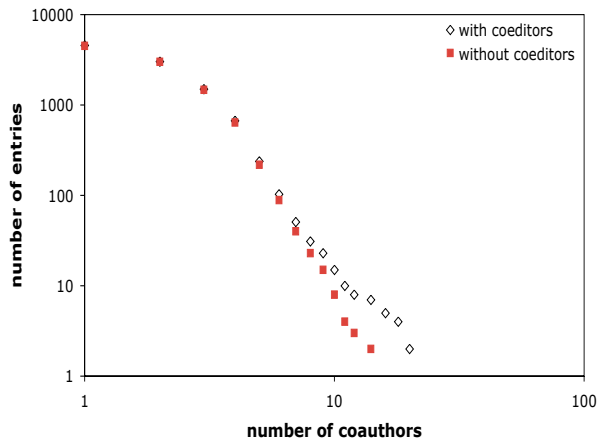


Figure 3: Cumulative distribution of the number of papers with a given number of coauthors on log-log scales.

component the average number of collaborators per author is 5.83 with co-editors and 4.39 without them.

The cumulative size distribution of the connected components with and without co-editors are depicted in Figure 4. Figure 4 shows that the probability density functions are well approximated by a power law with exponent of 2.9 (excluding co-editors) and 2.6 (total). Since the other authors did not provide the analogous data for their databases, we do not know how our figures would compare with those for other coauthorship databases.

The existence of a big connected component has a social meaning. It suggests 36.5% of GP researchers are members of a single community, since those researchers are either directly connected via a collaboration or they are close to each other in a way that will be made clear in section 3. The size of the giant component is notably smaller in the GP graph with respect to other measured coauthorship networks (see Table 1). This may be due to the comprehensive nature of the GP bibliography. It captures work done by smaller groups which does not get into major journals, whereas, perhaps, the other databases concentrate upon higher impact outlets where work is heavily cited but at the expense of ignoring less regarded authors. This may artificially inflate the fraction of authors within their giant component. Alternatively it may be due to the youth of the GP field, with many semi-isolated individuals and groups starting research independently.

One should also consider that all collaboration networks are in a non-equilibrium state as they are continuously evolving [3]. Accordingly, as time goes by, one should observe small components progressively connecting themselves to the large one. For example, in less than one year the size of the giant component including co-editors has grown from 942 to 1025 nodes. This is due in part to a number of newcomers collaborating with people already belonging to the giant component. The other part comes from the absorption of a few disconnected small components into the giant one thanks to one or more new collaborations. This suggests that the size of the giant component has not yet reached its “steady-state” value and it will continue to grow in relative

size. Since we possess all the time-stamped data, it is possible to study the evolution of this component, as well as several other indicators from the beginning and up to the present days. This investigation is currently under way.

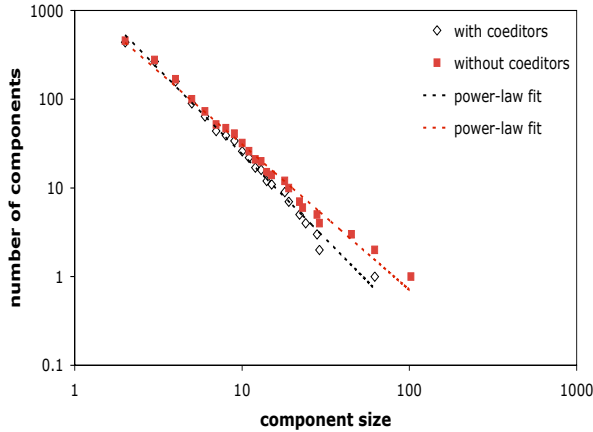


Figure 4: Cumulative distributions of the number of connected components in the collaboration graph by number of people. Log-log scale.

2.5 Social GP Clusters

The clustering coefficient of a node in a graph is the proportion of its neighbouring nodes which are also neighbours of each other. The average clustering coefficient $\langle C \rangle$ is calculated across all nodes in the graph [10]. In other words, $\langle C \rangle$ is a simple statistical measure of the amount of local structure that is present in a graph. Most real-world networks, e.g. the world wide web, roads, electrical power transmission and including the social networks that have been studied to date, have a much larger clustering coefficient than would be expected of a random graph with the same number of vertices and edges. Social networks are particularly clustered. For example, the average clustering coefficient is $\langle C \rangle = 0.665$ for the GP collaboration graph including book co-editors, and it is 0.660 without. (We would expect 0.0015 and 0.0013 for the corresponding random graphs). In terms of scientific collaborations, a high clustering coefficient means that people tend to collaborate in groups of three or more. This agrees with what we know of the GP field. It may mean that two researchers that collaborate independently with a third one may, in time, become acquainted and so collaborate themselves. Alternatively it might be due to collaborators coming from the same institution. In all cases, a high value of $\langle C \rangle$ for a social network is an indication that collaborations are not made at random at all, and that social forces and processes are at work in the network structure formation.

Table 1 summarises the results of this section and compares them with those for some other collaboration networks. Some of the entries in the table will be discussed in the following section. Most GP statistics are similar to those of the larger databases. However one notable difference, as we have already remarked, is the relative smallness of the largest component. The clustering is rather high, which shows that GP researchers know each other quite well within the large component, and the community is rather

homogeneous. In contrast, in biology and medicine or mathematics, where scientist from different sub-disciplines seldom collaborate, the clustering coefficient is lower. Note also the high number of authors per paper, and especially the strikingly high number of collaborators per author in the nuclear physics community (SPIRES). Clearly, nobody can maintain an average of 173 scientific partners on a first-hand acquaintance basis and thus this figure does not seem to be socially meaningful.

3. DISTANCES AND CENTRALITY

A social network can be characterised by a number of measures that give an idea of “how far” people are from each other, or how “central” they are with respect to the whole community. These measures are well known in social network analysis. Here we shall concentrate on *average path length* and on *betweenness centrality*.

3.1 Average Path Length

The average path length L of a graph is the average value of the shortest paths between all of its pairs of vertices. In random graphs and many real networks, such as the Internet, the World Wide Web and social networks, the average path distance scales as a logarithmic function $O(\log N)$ of the number of vertices N . Such networks, if they also have a high clustering coefficient, are known as *small worlds* networks [6]. Since, even for very large graphs, any two nodes in a small world network are only a few steps apart. In contrast in regular lattices, two nodes are $O(N^{1/D})$ apart. (Where D is the lattice’s dimensionality. For example, for a square lattice $L \leq \frac{2}{3}N^{1/2}$). The average path length of the giant component of the GP collaboration graph including coeditors is 4.74 (it is 5.2 without coeditors). The longest among all the shortest paths (known as the diameter) is 12 (14 without coeditors). Thus, unsurprisingly, the GP community, as far as its “core” component is concerned, is indeed a small world and is characterised by values that are typical of these kinds of network (see Table 1). Being a small world means that information may circulate quickly and collaborations are easier to set up. These are clearly advantageous for a research community. The connected components following the largest one are themselves small worlds. We expect over time some of them will merge with the largest component. (For this to happen, only a single new collaboration between two scientists each belonging to one of the components is needed.)

3.2 Betweenness

The betweenness $b(v)$ of a vertex v is the total number of shortest paths between all possible pairs of vertices that pass through this vertex. Nodes that have a high betweenness potentially have more influence, i.e. they are more central in the network, in that there is more “traffic” that goes through them. The first five authors in terms of betweenness in the network (including co-editors and in decreasing order) are: W. Banzhaf, H. Iba, U.-M. O’Reilly, H. de Garis and W. B. Langdon. W. Banzhaf is also the researcher that has the highest number of different collaborators. Without co-editors the ranking is: W. B. Langdon, U.-M. O’Reilly, W. Banzhaf, M. Tomassini and P. Nordin. People who have a large value of betweenness play the role of intermediaries or “brokers” in a social sense.

Table 1: Basic statistics for some scientific collaboration networks. GP1 is the GP bibliography at the start of 2007, including coedited books and proceedings. GP2 is the same but without coeditors. SPIRES is a data set of papers in high-energy physics. Medline is a database of articles on biomedical research. Mathematics comprises articles from *Mathematical Reviews*. NCSTRL is a database of preprints in computer science. Physics has been assembled from papers posted on the Physics E-print Archive. Details about these databases can be found in [5, 7, 8].

	GP1	GP2	SPIRES	Medline	Mathematics	NCSTRL	Physics
Total number of papers	4564	4504	66652	2163923	1600000	13169	98502
Total number of authors	2809	2765	56627	1520251	253339	11994	52909
Average papers per author	3.16	3.14	11.6	6.4	7	2.55	5.1
Average authors per paper	2.25	2.22	8.96	3.754	1.5	2.22	2.53
Average collaborators per author	4.17	3.62	173	18.1	2.94	3.59	9.7
Size of the giant component (%)	36.5	26.9	88.7	92.6	82.0	57.2	85.0
Clustering coefficient	0.665	0.660	0.726	0.066	0.15	0.496	0.43
Average path length	4.74	5.2	4.0	4.6	7.73	9.7	5.9

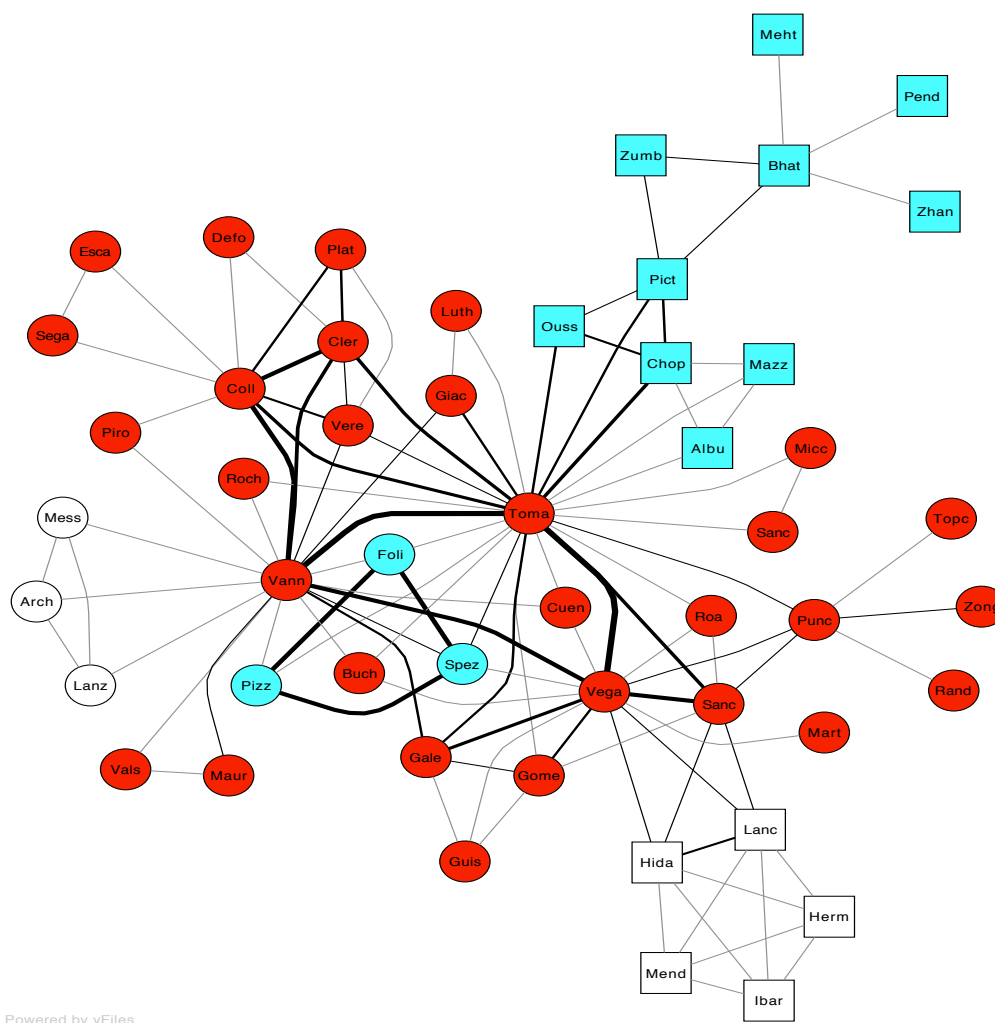


Figure 5: One of the communities belonging to the main network component. The thickness of the links gives an indication of the number of co-authored papers. The largest thickness indicates more than 16 coauthored works. The thinnest link (light gray) stands for a single collaboration. The different symbols and colours represent sub-communities of the illustrated community.

3.3 Non-random collaborations between directly connected authors

Most technological and biological networks are disassortive in that they have negative correlation, meaning that high-degree vertices are preferentially connected to low-degree vertices. However most measured social networks are assortative, meaning highly connected nodes tend to be connected with other highly connected nodes [10]. The GP collaboration network confirms this general observation with a correlation coefficient of +0.15 for the giant component, and +0.30 for the whole graph (including coeditors and excluding the single physicist’s paper). These are close to the coefficients observed for other social networks (specifically 0.127 for Medline and 0.120 for Mathematics [9]).

4. COMMUNITIES IN THE GIANT COMPONENT

All the researchers belonging to the largest component of the network can be said to form part of the GP community at large, in the sense that they are all only a few steps away from any other member of the community. However, we know from direct experience that some groups of GPer are more closely connected between themselves than with other people. In other words, they belong to what one might call a group or a tighter community within the global one. It is not easy to give a rigorous quantitative definition of a community within a network. For our purposes a community can be seen as a set of highly connected vertices having few connections with vertices belonging to other communities. In the analysis of social networks, several algorithms that attempt to split a network into communities have been proposed. We used Newman’s method [11], which is based on a measure of the fraction of edges that fall within communities minus the expected value of the same quantity if edges fall at random without regard for the community structure.

Since the GP bibliography contains the number of papers that any two collaborators have published together, it is possible to go a step further than just saying that two people have coauthored at least a paper, and give a measure of the *intensity* of the collaboration. We use the number of papers that two given authors have in common as a measure of the strength of their collaboration. Newman [8] has proposed a more refined measure which takes into account the actual number of coauthors of each paper. However this is more complicated than we need, instead we ignore the total number of coauthors for each paper. Our measure of collaboration strength is used in our communities algorithm to highlight groups of researchers that have collaborated strongly with the aim of uncovering the stability of the scientific relationship. We have also excluded coedited proceedings, books, etc., as we have already seen that these might sometimes represent spurious collaboration relationships.

The results of running the algorithm on the subgraph represented by the largest connected component are qualitatively surprisingly close to what one would expect, given our knowledge of the GP field. The advantage is that the analysis makes them explicit and uncovers a number of other relationships that would be difficult to infer without an explicit study of the raw data. As an example of the about 25 communities that the algorithm discovers, Figure 5 shows the structure of the groups around one of us (“Toma”). If

we now consider this community as an isolated subgraph and apply again Newman’s algorithm to it, we obtain the groups highlighted by different symbols and colours in the figure. Thus, the groups correspond to sub-communities within the main community. The thickness of the links represents the intensity of the relationship. It is easy to recognise a “hard core” of collaborating researchers strongly connected to “Toma” forming triads and higher polygons of order four and five. The strong triangle (“Foli”, “Pizz”, “Spez”) is relatively loosely connected to the rest, showing that these researchers belong to the community but often collaborate between themselves. It is also possible to discern institutional and geographical components in the community. For example, most of the upper right part of the figure through the node “Chop” comprises researchers essentially belonging to the University of Geneva, which is close to the University of Lausanne, to which “Toma” belongs. However, geographical closeness is not the key factor in the other groups which belong to Universities in France, Italy, Spain, and the US. We might conjecture that many collaborations start locally at the same or at close institutions and then they spread through people being introduced to others via a common acquaintance, or through people physically moving or visiting other institutions. This is the case in the figure, where “Vann”, “Chop”, and “Vega” among others have played the role of “bridges” between different institutions and across countries.

As a second illustration, let us look at Figure 6 which is the community that revolves around one of us (“Lang”) and “Poli”. In contrast to the previous case, one can see that the graph structure is more “star-like”, with two large directly connected big hubs (“Lang” and “Poli”) who have about 70 co-authored papers, and three other highly connected nodes (“Buxt”, “McPh”, “Rowe”) which are strongly connected to one of the main hubs but not to both. It is interesting to observe the role of “McPh” who, like “Vega” in the previous community (cf. Figure 5), plays a bridging role, this time between some UK and some American researchers. We can also recognise a strong “theory-oriented” group, which is almost a clique in the graph, formed by (“McPh”, “Poli”, “Rowe”, “Steph”, “Wrig”). There is also another bridge formed by “Cagn” from UK to Italy, again due to a long-standing collaboration and friendship. The small cliques or almost cliques at the periphery of the figure essentially represent people that have worked at the same institution in either Italy or the US.

The discussion above, motivated by our belonging to the mentioned communities, and thus by our direct human knowledge about them, should be enough to get an impression of the many useful observations that one can make on the communities that interlock in the main network component. There are of course several other large well known and interesting communities in the network but unfortunately we cannot describe them here for reasons of space³.

5. CONCLUSIONS

In sections 2 and 3 we characterised the genetic programming (GP) coauthorship graph using a number of local and global statistics. We extended and updated the findings presented in [13] by studying the influence of coedited volumes

³interested readers can contact one of the authors if they wish to know more about these communities.

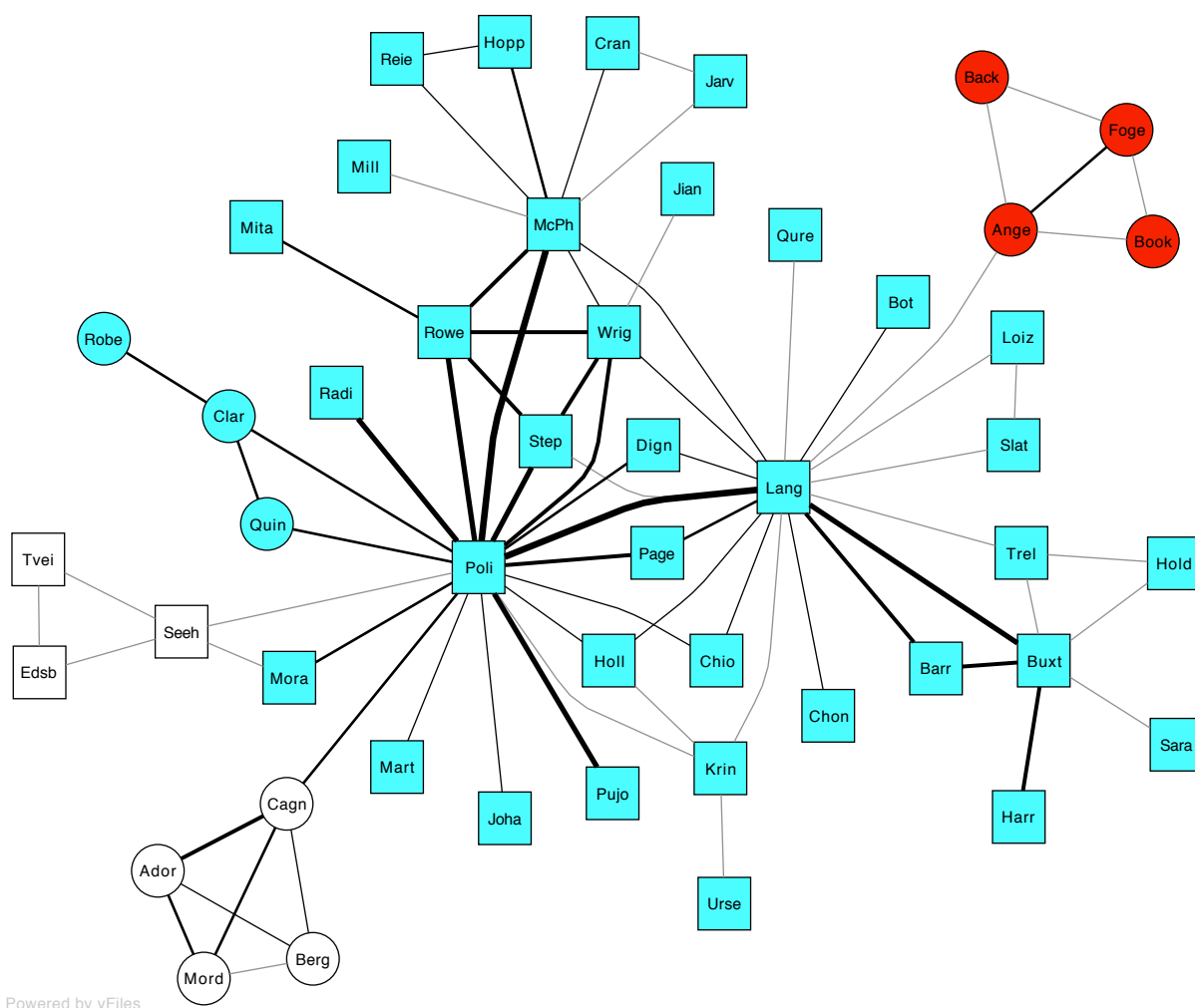


Figure 6: Another community belonging to the main network component. The thickness of the links gives an indication of the number of co-authored papers. The largest thickness indicates more than 16 coauthored works. The thinnest link (light gray) stands for a single collaboration. The different symbols and colours represent sub-communities.

and by using the latest data available. Section 3 showed the GP field to be highly clustering and that the GP coauthorship network has a small mean path length. Together these suggest that, at least for the core, GP is indeed a “small world”. We also found, compared with other published collaboration networks, that the fraction of GP authors connected by coauthorship is a relatively small fraction of all GP authors.

Section 4 is a study of the community structure of GP. It uses a more precise definition of collaboration, which takes into account the intensity of the relationship. This uncovers many groups of tightly interacting researchers. From the detailed study of two of the communities we have drawn inferences about the pivotal role of some researchers or groups of researchers in promoting collaborations within and between academic institutions. Adding our human knowledge about geographical location and personal acquaintance, allows some conjectures to be drawn about the way in which

different continents and countries collaborate on research projects.

It should be obvious that the present data driven approach to social network analysis can only provide some answers but not all of them. Algorithms and data cannot take into account human aspects such as friendship in scientific collaboration. While these may be buried in the sea of numbers they will never appear explicitly from such analyses. Nevertheless, we feel that our results are interesting and useful in the way that they characterise our community.

There is another aspect of the collaboration graph that would be revealing: the analysis of its development over the years. Indeed, since each paper has a date of publication, we possess all the data that are needed for such an investigation. This would allow the detailed study of how the network has grown to its present size and structure from the beginning and might give hints as to its future progress. This extension is currently under investigation.

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